

A yellow line representing a seismic waveform. It starts with a vertical line, then shows several small oscillations, followed by a larger, more complex oscillation, and finally a series of smaller, decaying oscillations.

**Ground motion parameters  
based on evolution of intensity and  
frequency content with time**

**Sanaz Rezaeian, USGS**

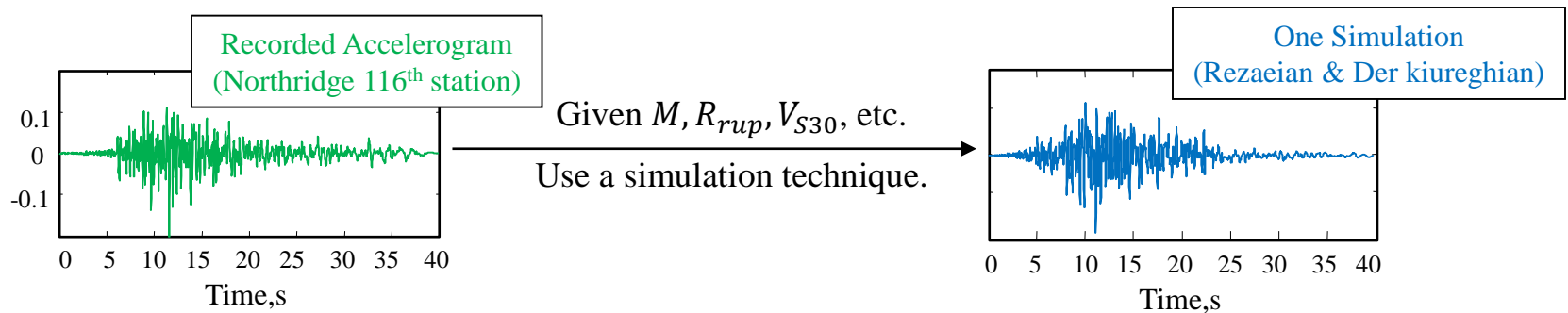
**Farzin Zareian, Peng Zhong, UCI**

Workshop on Implementation of GMSV Gauntlets on the Broadband Platform  
February 29, 2016

# Rezaeian et al. Time-Domain Ground Motion Parameters:

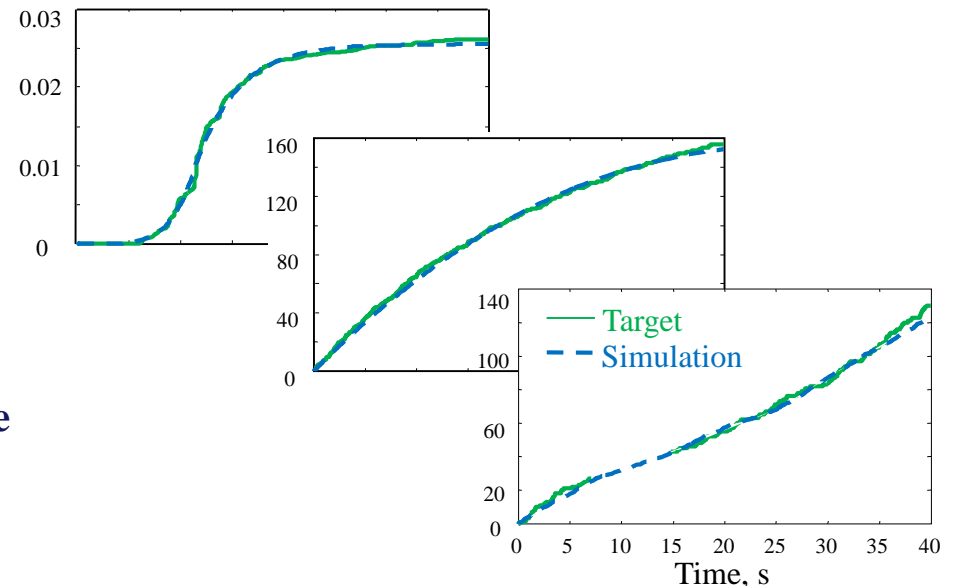
# Scope:

Statistical characteristics of ground motion time-series can be used to represent variations of the **intensity** and the **frequency content** over time. These features are compared for recorded and simulated motions.



## Three Time-Domain Parameters:

- 1) Compare the **cumulative intensity**,  $\int a^2 dt$   
(a measure of the **evolutionary intensity**)
- 2) Compare the **cumulative number of zero-level up-crossings**  
(a measure of **predominant frequency**)
- 3) Compare the **cumulative number of positive minima and negative maxima**  
(a measure of **bandwidth**)

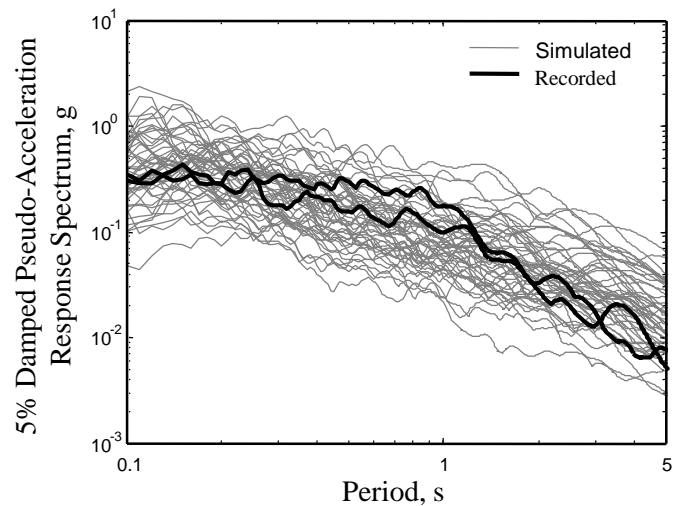


# Scope:

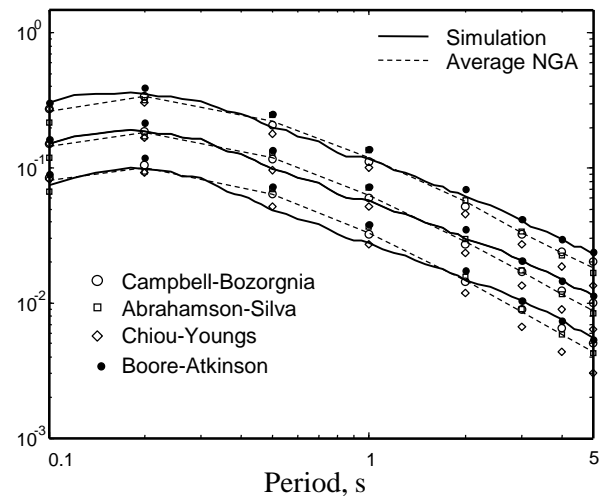
In a previous study, simulations that were based on matching these three metrics were validated against recorded motions and GMPEs in terms of response spectrum.

## Elastic Response Spectrum:

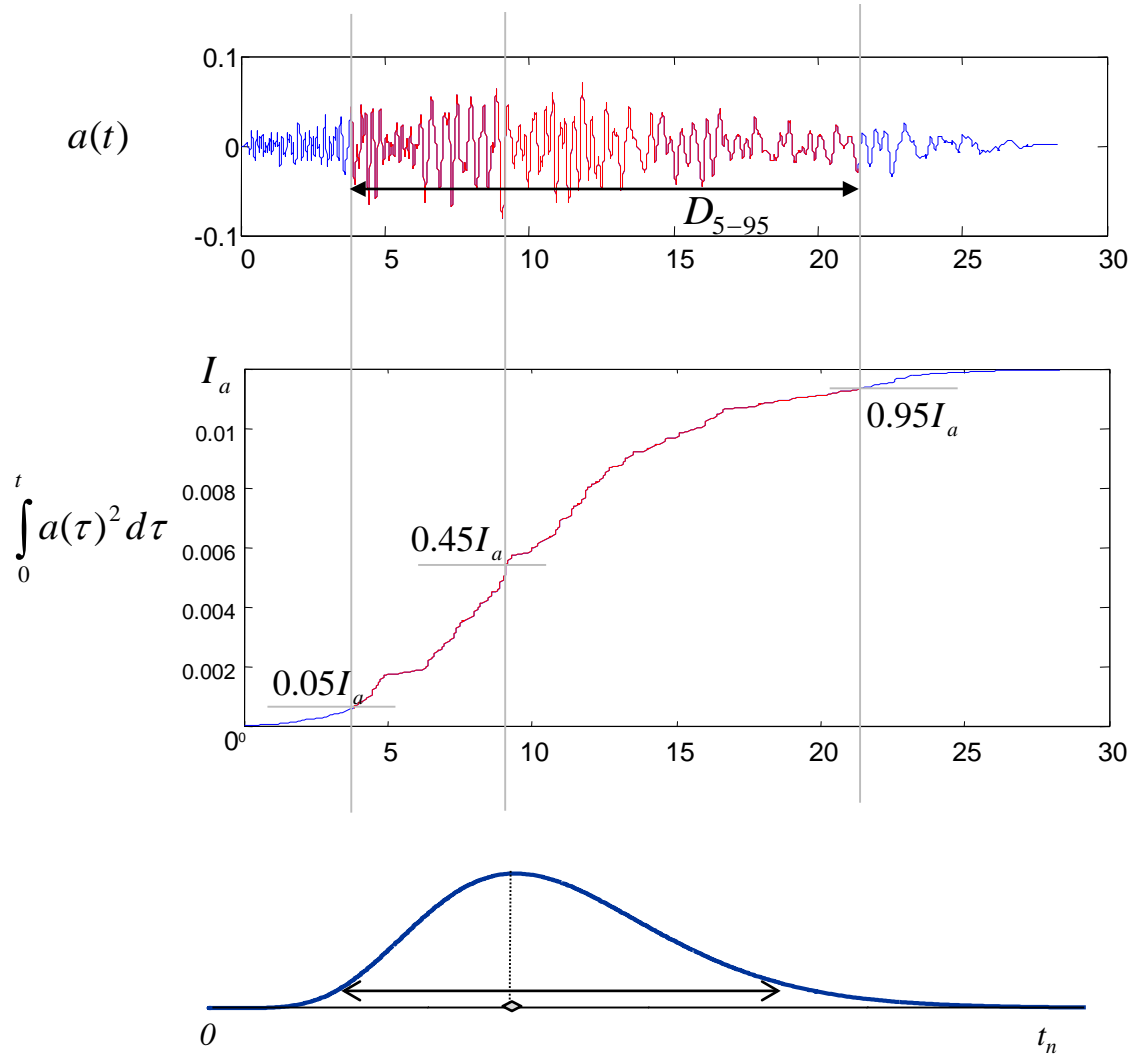
50 simulations for  $F_{rv}, M, R_{rup}, V_{S30}$   
(1, 6.69, 20.3, 1223) of the recorded motion.



Median ( $\pm 1$ std) of 500 simulations  
 $(F_{rv}, M, R_{rup}, V_{S30}) = (0, 7.0, 40, 760)$



# Evolution of Intensity (parameter 1):



## Scalar Parameters:

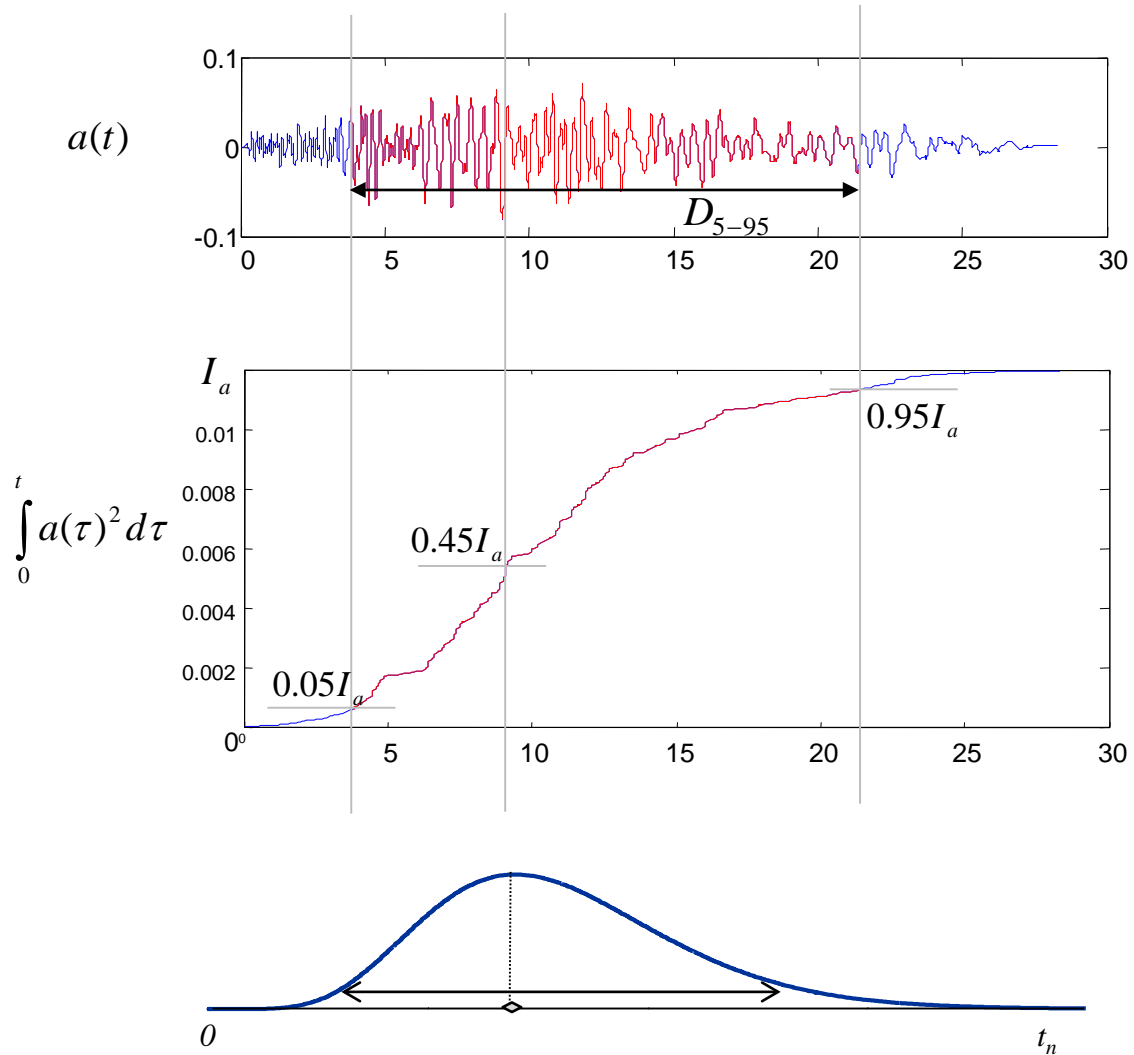
$$I_a = \frac{\pi}{2g} \int_0^{t_n} a^2 dt \quad : \text{Arias intensity}$$

$D_{5-95}$  : Effective duration  
(from 5% to 95%  $I_a$ )

$\frac{I_a}{D_{5-95}}$  : Rate of input energy

$t_{mid}$  : Middle of strong shaking  
(~ at 45%  $I_a$ )

# Evolution of Intensity (parameter 1):



## Scalar Parameters:

$$I_a = \frac{\pi}{2g} \int_0^{t_n} a^2 dt \quad : \text{Arias intensity}$$

$D_{5-95}$  : Effective duration  
(from 5% to 95%  $I_a$ )

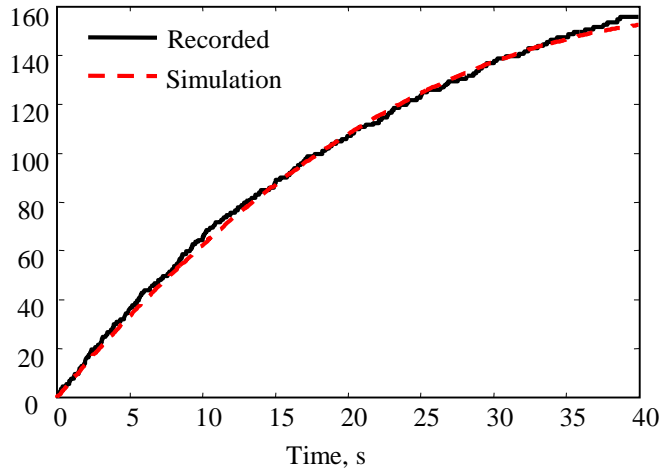
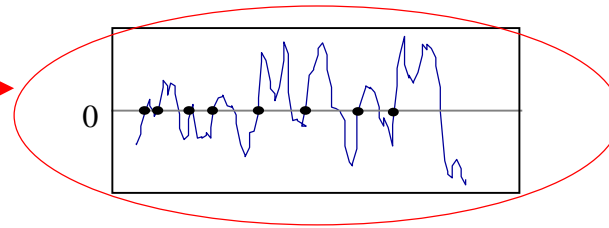
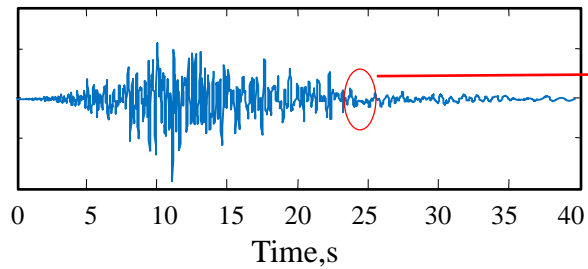
$$\frac{I_a}{D_{5-95}} \quad : \text{Rate of input energy}$$

$t_{mid}$  : Middle of strong shaking  
(~ at 45%  $I_a$ )

# Evolution of Frequency (parameter 2):

A measure of predominant frequency:

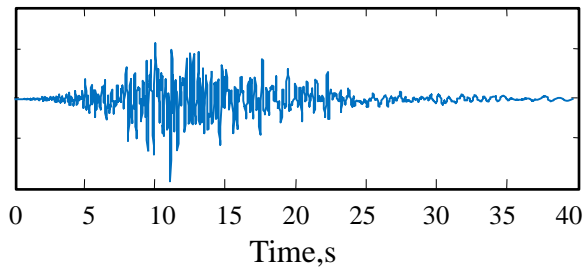
Cumulative number of zero-level up crossings



# Evolution of Frequency (parameter 2):

A measure of predominant frequency:

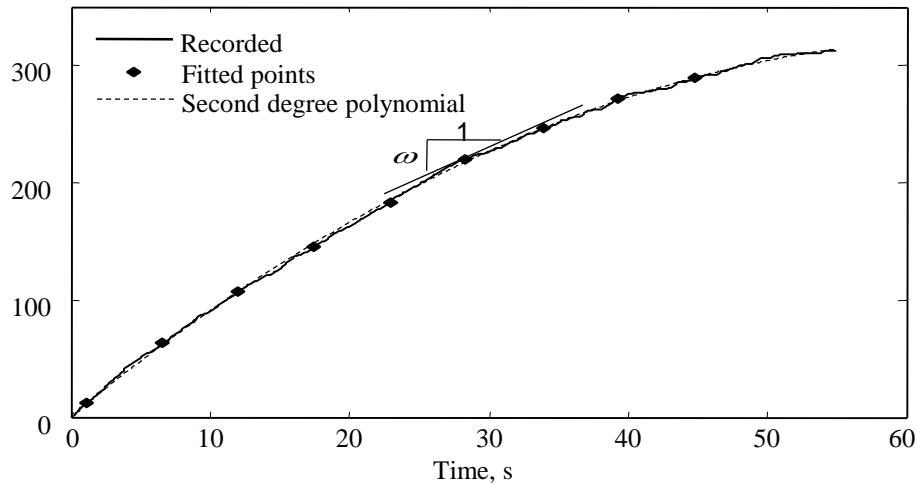
Cumulative number of zero-level up crossings



## Scalar Parameters:

$\omega_{mid}$  : Frequency of strong shaking phase

$\omega'$  : Rate of change of frequency

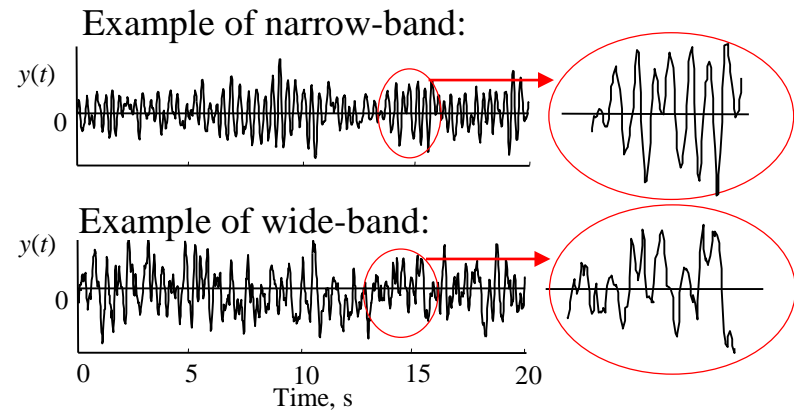
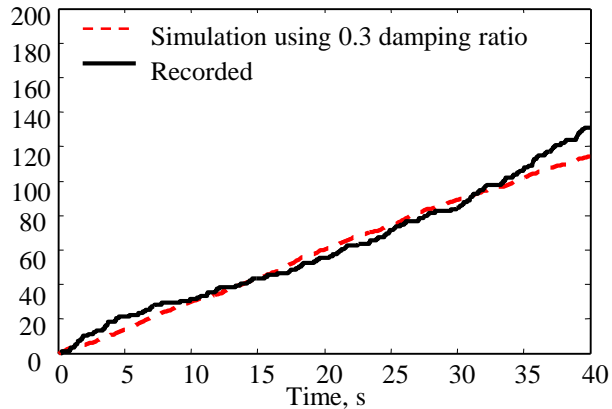
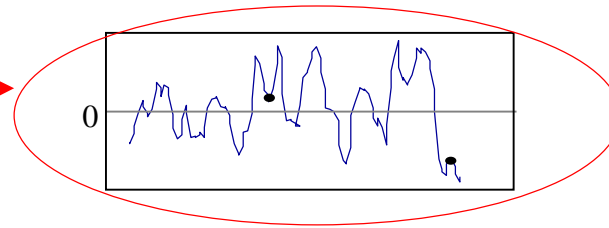
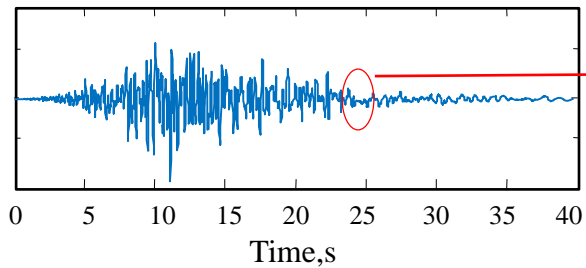




# Evolution of Bandwidth (parameter 3):

**A measure of bandwidth:**

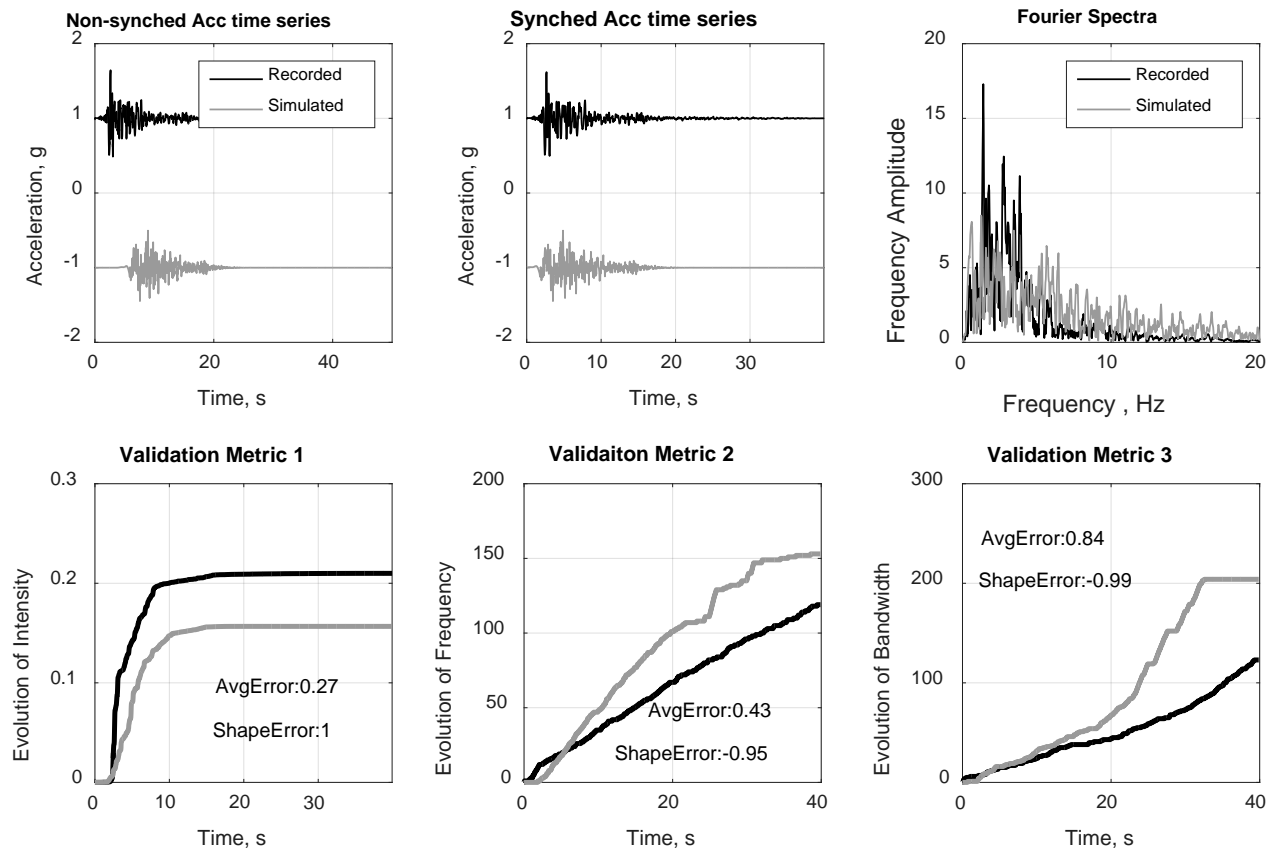
Cumulative number of positive minima and negative maxima



# Summary:

A validation gauntlet using evolution of intensity and frequency content of ground motion waveform. Explains discrepancies in response (including and) beyond elastic spectra and duration.

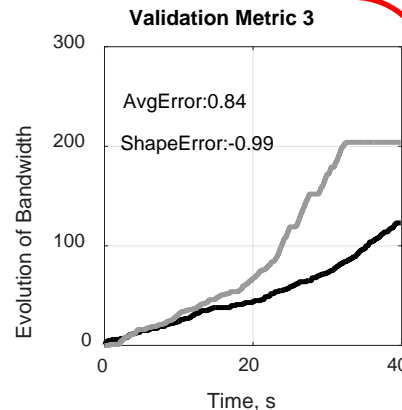
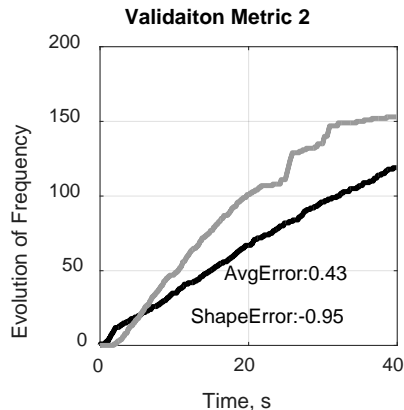
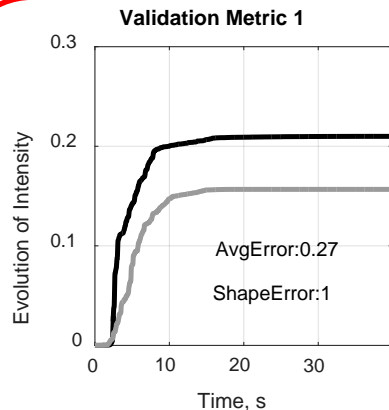
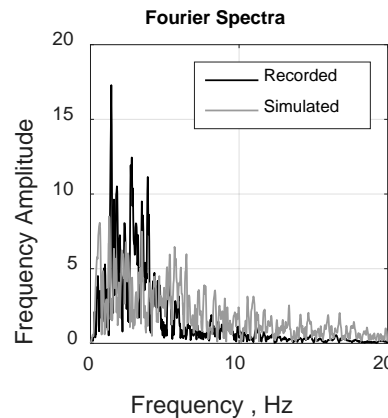
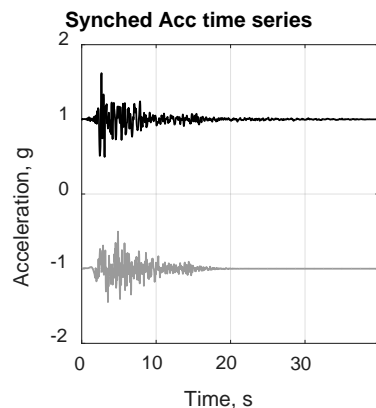
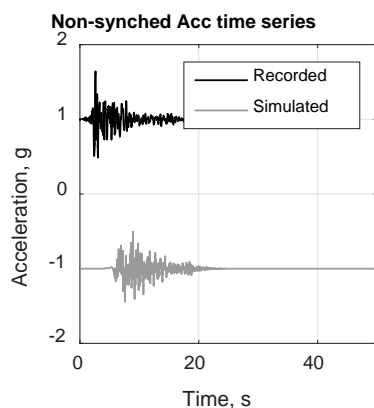
Example Output for Visual Inspection:



# Summary:

A validation gauntlet using evolution of intensity and frequency content of ground motion waveform. Explains discrepancies in response (including and) beyond elastic spectra and duration.

Example Output for Visual Inspection:

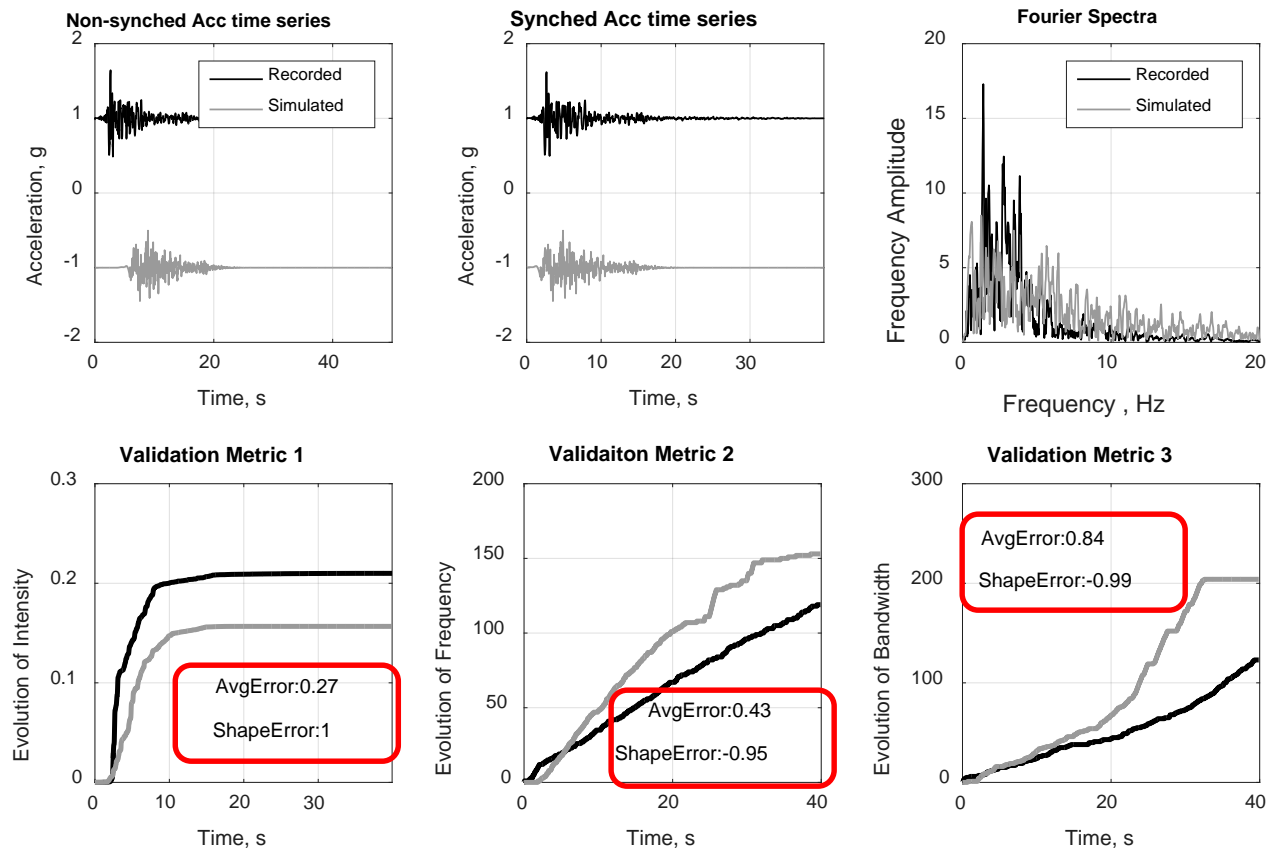


For Visual Inspection:  
(model developers, individual records)  
1) Evolution of intensity  
2) Evolution of predominant frequency  
3) Evolution of bandwidth

# Summary:

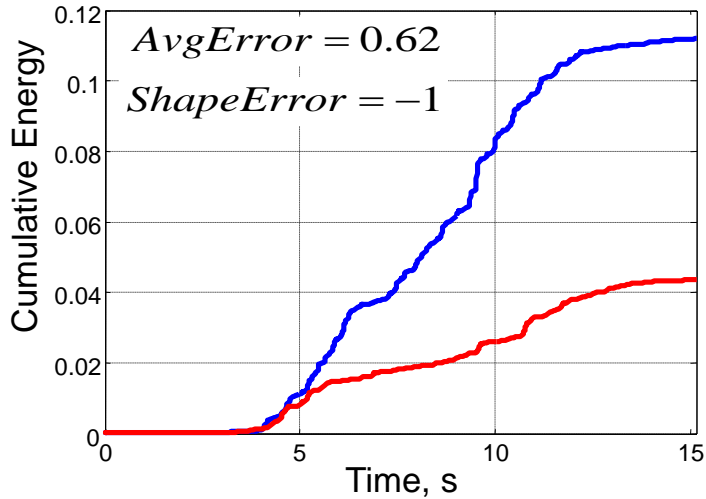
A validation gauntlet using evolution of intensity and frequency content of ground motion waveform. Explains discrepancies in response (including and) beyond elastic spectra and duration.

Example Output for Visual Inspection:



Quantified Errors -- Scalars:  
(engineers, large number of records)  
1) Average Error  
2) Shape Error

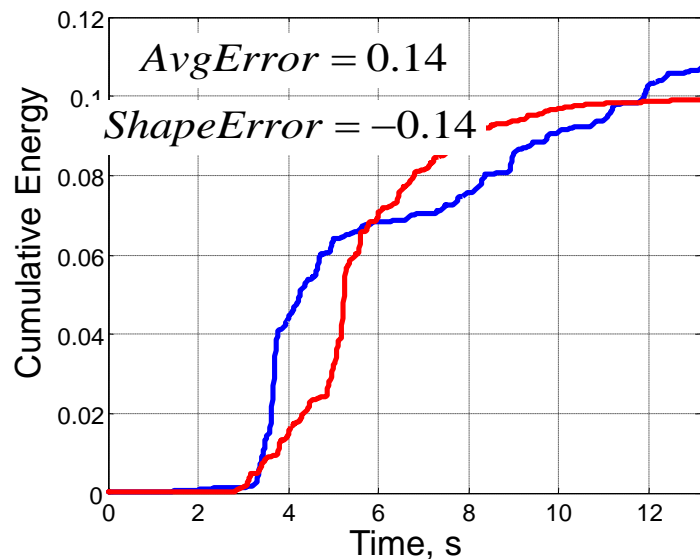
# Scalar Error Terms :



Avg Error:

$$e_{ij} = \frac{\int_0^{t_n} |m_{ij,\text{rec}}(t) - m_{ij,\text{siml}}(t)| dt}{\int_0^{t_n} m_{ij,\text{rec}}(t) dt},$$

$i = 1, 2, 3; \quad j = 1, \dots, \text{number of simulations}$



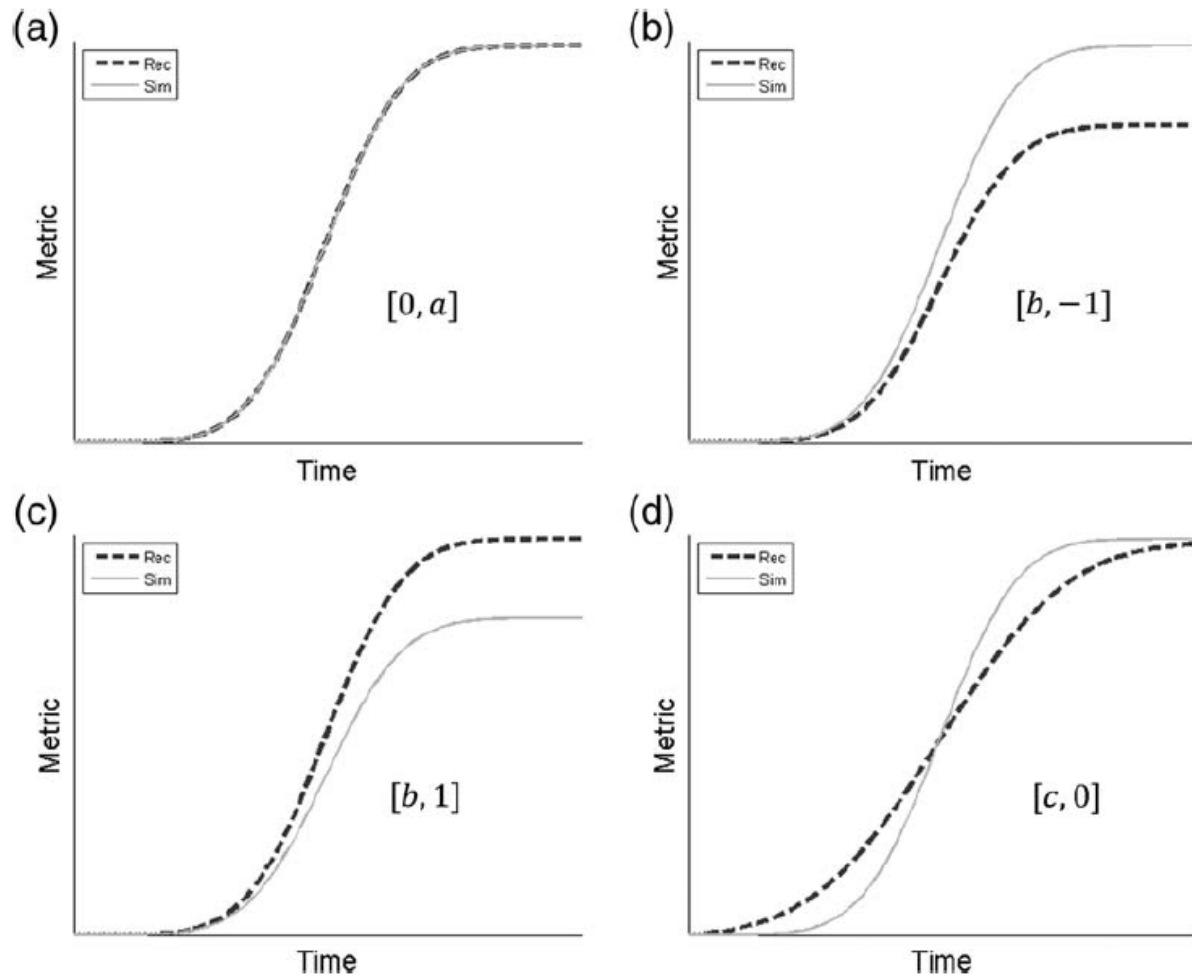
Shape Error:

$$v_{i,j} = \frac{\int_0^{t_n} (m_{ij,\text{rec}}(t) - m_{ij,\text{siml}}(t)) dt}{\int_0^{t_n} |m_{ij,\text{rec}}(t) - m_{ij,\text{siml}}(t)| dt},$$

$i = 1, 2, 3; \quad j = 1, \dots, \text{number of simulations.}$

# Scalar Error Terms :

[Avg Error , Shape Error]



# For More Details :

**Rezaeian et al. (2015) BSSA Journal:**

Bulletin of the Seismological Society of America, Vol. 105, No. 6, pp. 3036–3049, December 2015, doi: 10.1785/0120140210

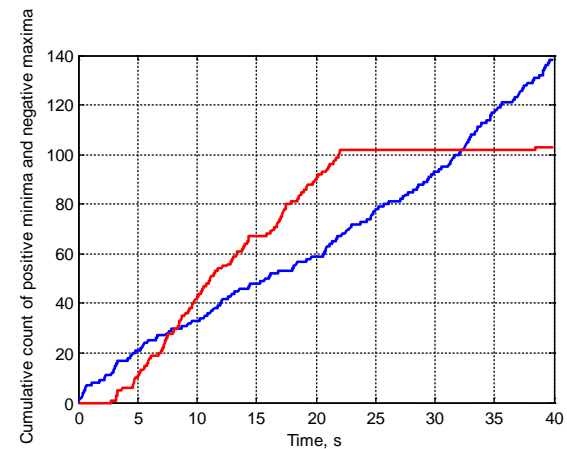
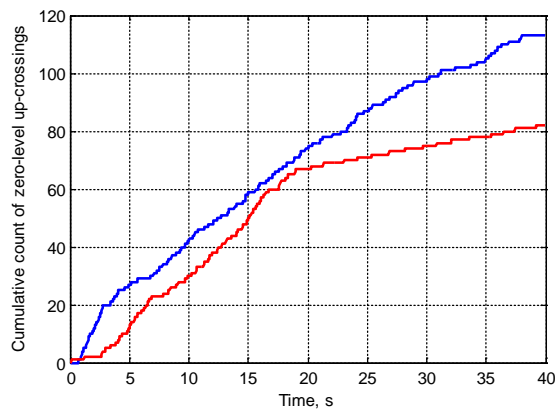
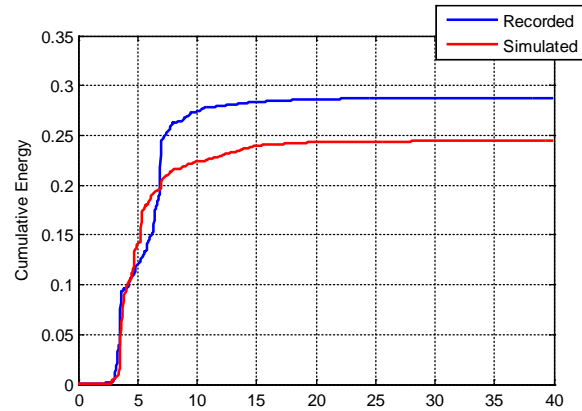
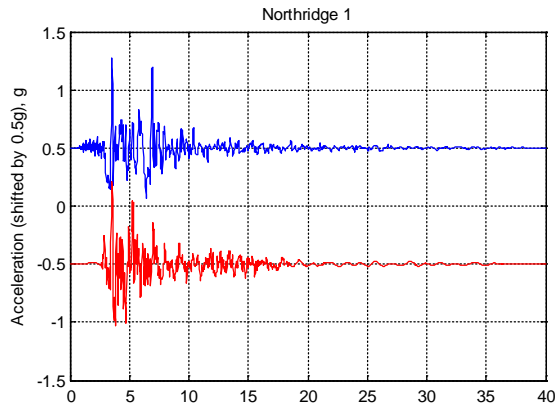
## Validation of Simulated Earthquake Ground Motions Based on Evolution of Intensity and Frequency Content

by Sanaz Rezaeian, Peng Zhong, Stephen Hartzell, and Farzin Zareian

**Abstract** Simulated earthquake ground motions can be used in many recent engineering applications that require time series as input excitations. However, applicability and validation of simulations are subjects of debate in the seismological and engineering communities. We propose a validation methodology at the waveform level and directly based on characteristics that are expected to influence most structural and geotechnical response parameters. In particular, three time-dependent validation metrics are used to evaluate the evolving intensity, frequency, and bandwidth of a waveform. These validation metrics capture nonstationarities in intensity and frequency content of waveforms, making them ideal to address nonlinear response of structural systems. A two-component error vector is proposed to quantify the average and shape differences between these validation metrics for a simulated and recorded ground-motion pair. Because these metrics are directly related to the waveform char-

# Example :

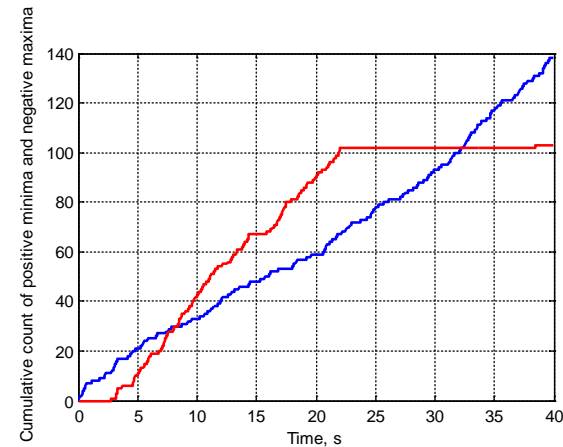
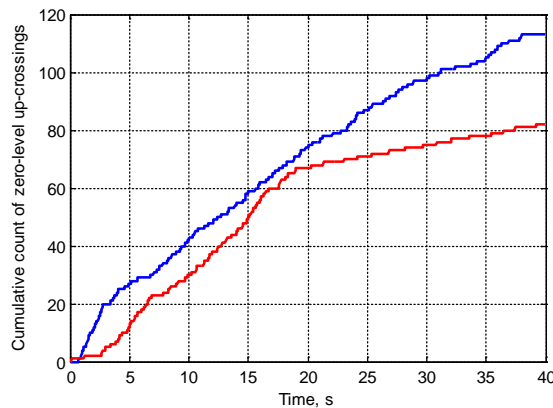
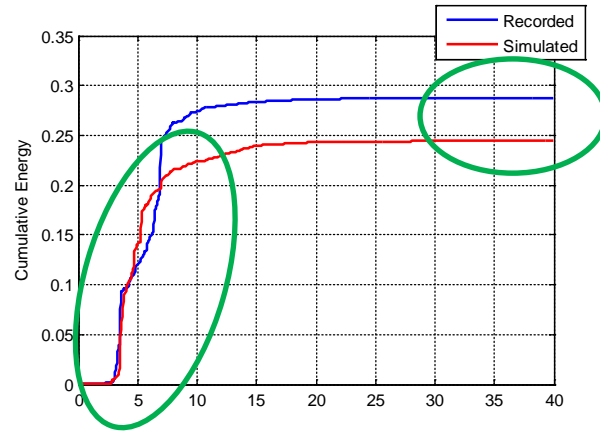
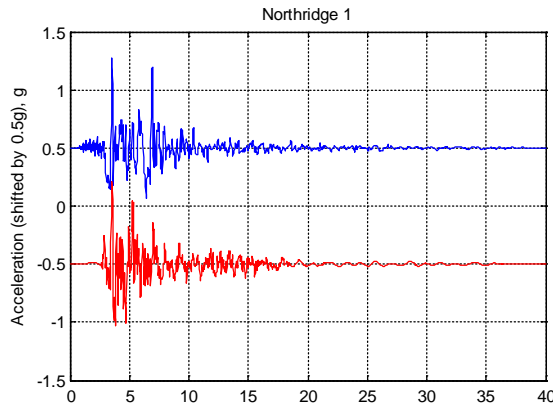
Use for Visual Inspection by Model Developers:





# Example :

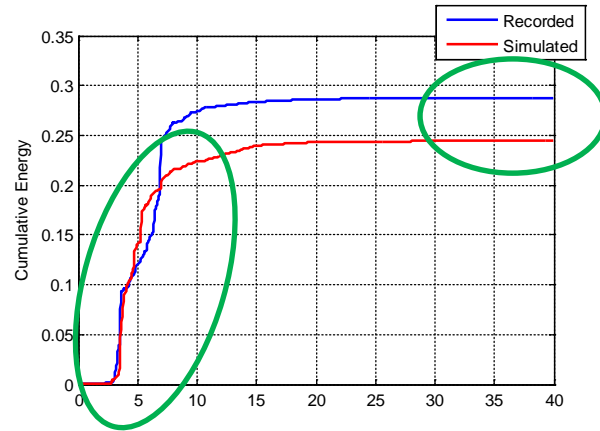
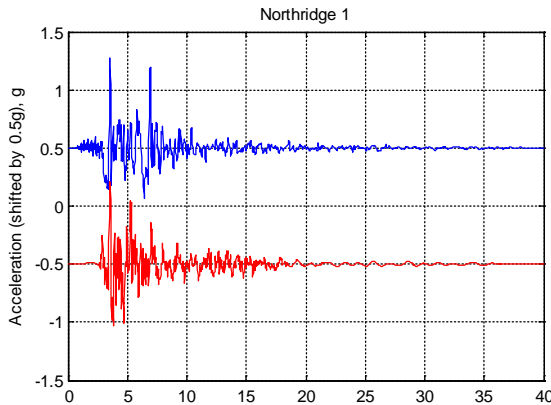
Use for Visual Inspection by Model Developers:



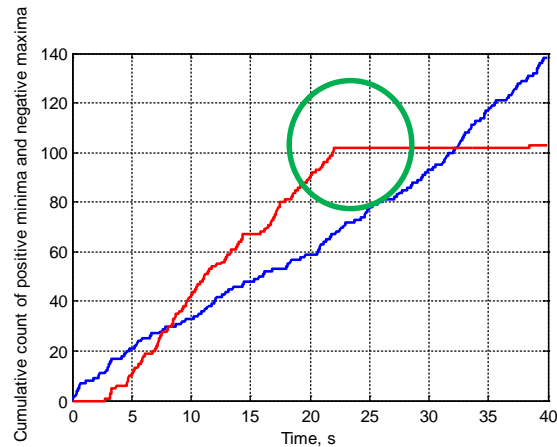
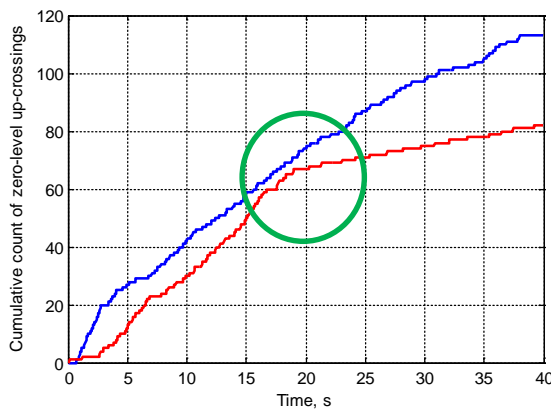
Evolution of  
Intensity

# Example :

Use for Visual Inspection by Model Developers:



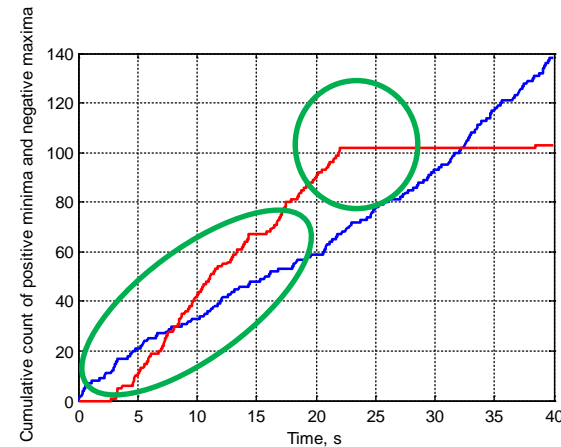
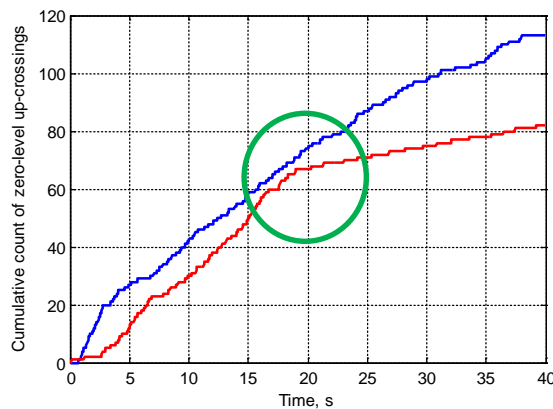
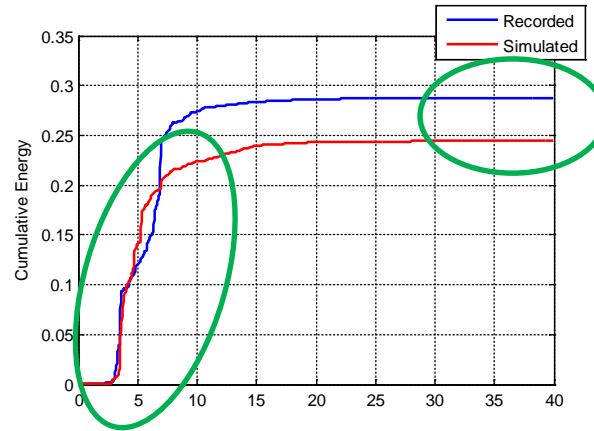
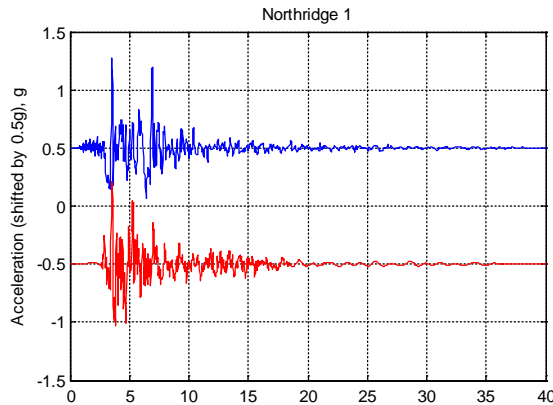
Evolution of Intensity



Discontinuity in frequency

# Example :

Use for Visual Inspection by Model Developers:



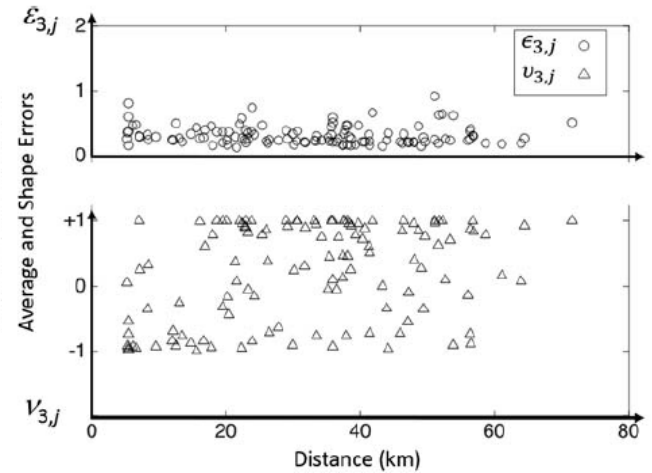
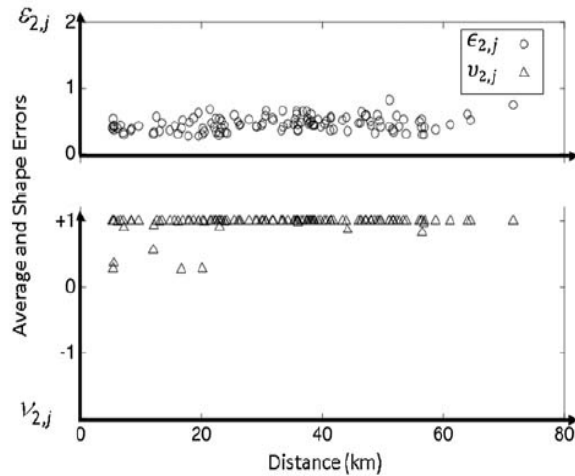
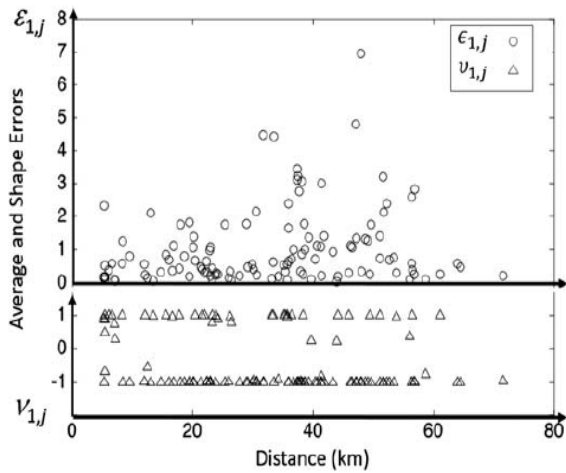
Evolution of Intensity

Discontinuity in frequency

Higher Bandwidth

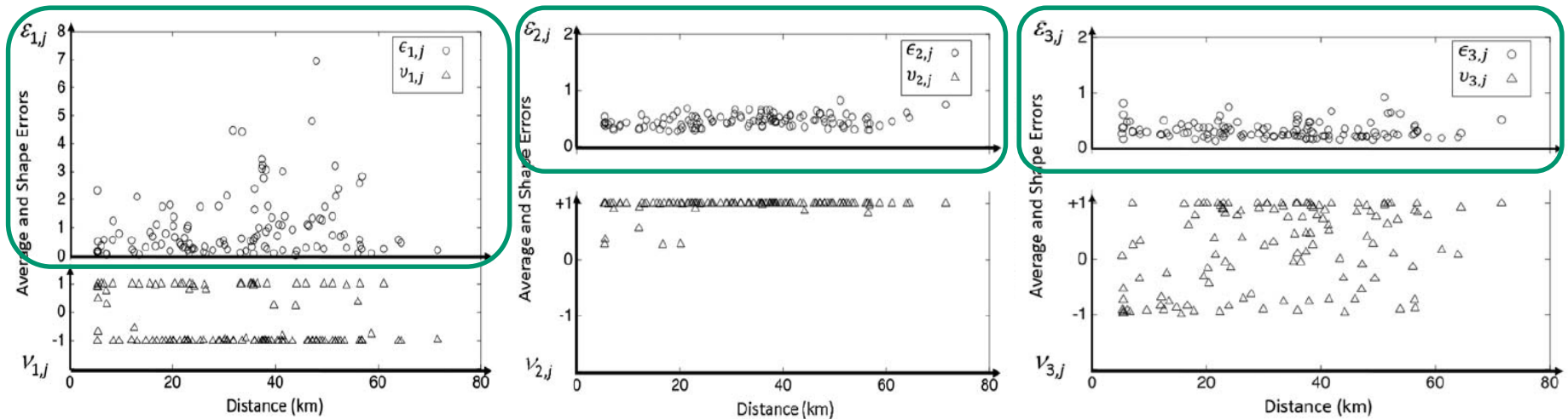
# Example :

Use of error terms for assessing a large number of simulations:



# Example :

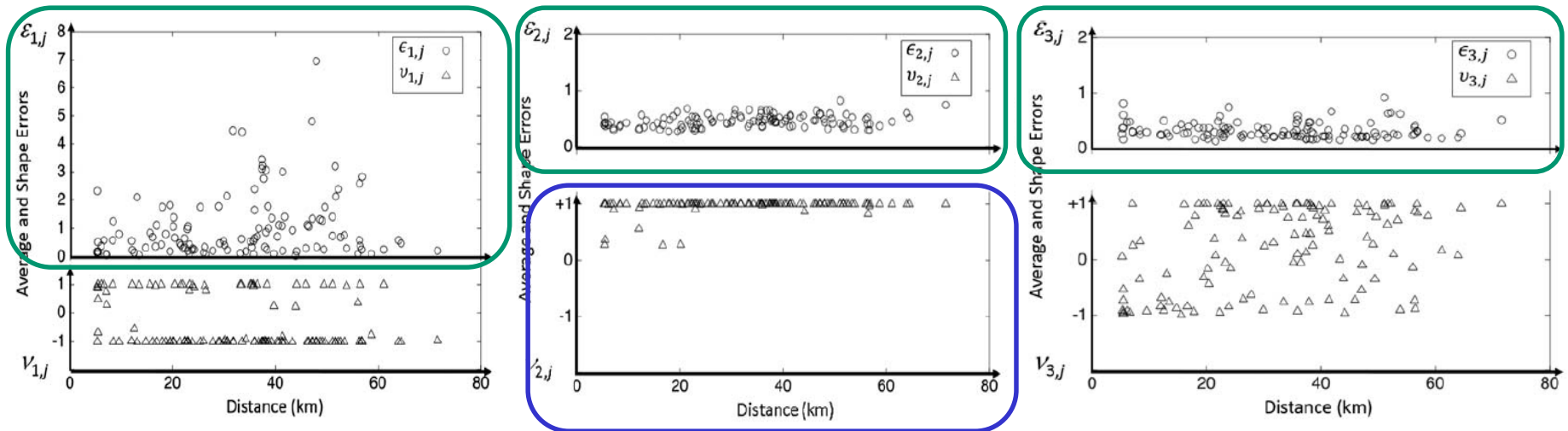
Use of error terms for assessing a large number of simulations:



Note: A relative validation method

# Example :

Use of error terms for assessing a large number of simulations:



Note: A relative validation method

In general, underestimating metric 2 (frequency and how it changes with time)